

Concours de l'Institut

encours

$$1. (2x-1)(3x+2) - (x-3)(3x+2) = 0$$

$$(3x+2)[(2x-1) - (x-3)] = 0$$

$$(3x+2)(2x-1-x+3) = 0$$

$$(3x+2)(x+2) = 0$$

$$\text{Smt } 3x+2 = 0$$

$$\boxed{x = -\frac{2}{3}}$$

$$\text{Smt } x+2 = 0$$

$$\boxed{x = -2}$$

$$2. (x-1)(4x+3) = (2x+1)^2$$

$$4x^2 + 3x - 4x - 3 = 4x^2 + 4x + 1$$

$$3x - 4x - 4x = 1 + 3$$

$$-5x = 4$$

$$\boxed{x = -\frac{4}{5}}$$

$$3. (3x+1)^2 - (2x+3)^2 = 0$$

$$[(3x+1)+(2x+3)][(3x+1)-(2x+3)] = 0$$

$$[3x+1+2x+3][3x+1-2x-3] = 0$$

$$(5x+4)(x-2) = 0$$

$$\text{Smt } 5x+4 = 0$$

$$\boxed{x = -\frac{4}{5}}$$

$$\text{Smt } x-2 = 0$$

$$\boxed{x = 2}$$

$$4. \frac{5-x}{x+2} = 2 \Rightarrow 5-x = 2(x+2)$$

$$5-x = 2x+4$$

$$-x-2x = 4-5$$

$$-3x = -1$$

$$\boxed{x = \frac{1}{3}}$$

$$5. 2x+1 = \frac{4}{2x+1}$$

$$(2x+1)^2 = 4$$

$$(2x+1)^2 - 2^2 = 0$$

$$(2x+1+2)(2x+1-2) = 0$$

$$(2x+3)(2x-1) = 0$$

$$\text{Smt } 2x+3 = 0 \quad \text{Smt } 2x-1 = 0$$

$$\boxed{x = -\frac{3}{2}}$$

$$\boxed{x = \frac{1}{2}}$$

$$6. \frac{3x+1}{2} - \frac{4x-1}{5} = \frac{2x-1}{10} + x$$

$$\frac{5(3x+1)}{10} - \frac{2(4x-1)}{10} = \frac{2x-1}{10} + \frac{10x}{10}$$

$$15x+5 - 8x+2 = 2x-1+10x$$

$$15x - 8x - 2x - 10x = -1 - 2 - 5$$

$$-5x = -8$$

$$\boxed{x = -\frac{8}{5}}$$

exo2

$$1. f(x) = x^2 - 2x + (2x)^2 - (3 - 3x - 6x + 6x^2)$$

$$f(x) = x - 6x + 6x^2 - 3 + 3x + 6x - 6x^2$$

$$f(x) = -2x^2 + 5x - 2$$

$$\begin{aligned} 2. f(x) &= (-1+2x)^2 - (3-6x)(1-x) \\ &= (-1+2x)(-1+2x) - 3(1-2x)(1-x) \\ &= -(1-2x)(-1+2x) - 3(1-2x)(1-x) \\ &= (1-2x)[-(-1+2x) - 3(1-x)] \\ &= (1-2x)[1-2x - 3 + 3x] \\ &= (1-2x)(x-2) \end{aligned}$$

$$3. a. f(x) = 0$$

$$(1-2x)(x-2) = 0$$

$$\text{Soit } 1-2x = 0$$

$$\boxed{x = \frac{1}{2}}$$

$$\text{Soit } x-2 = 0$$

$$\boxed{x = 2}$$

$$b. f(x) = -2$$

$$-2x^2 + 5x - 2 = -2$$

$$-2x^2 + 5x = 0$$

$$x(-2x+5) = 0$$

$$\text{Soit } \boxed{x=0} \quad \text{Soit } -2x+5=0$$

$$\boxed{x = \frac{5}{2}}$$

$$c. f(x) = x-2$$

$$(1-2x)(x-2) = x-2$$

$$(1-2x)(x-2) - (x-2) = 0$$

$$(x-2) [(1-2x) - 1] = 0$$

$$(x-2)(-2x) = 0$$

$$\text{Soit } x-2 = 0$$

$$\boxed{x = 2}$$

$$\text{Soit } -2x = 0$$

$$\boxed{x = 0}$$

exo3

P1 x : salaire d'un ouvrier

$x+400$: salaire contremaître

$x+1400$: salaire Patron.

$$\text{On pose } 11x + 2(x+400) + x+1400 = 19000$$

$$11x + 2x + 800 + x + 1400 = 19000$$

$$14x + 2200 = 19000$$

$$14x = 16800$$

$$x = \frac{16800}{14}$$

$$x = 1200$$

Dmc ouvrier : 1200 € contremaître : 1600 € Patron : 2600 €

P2

	Aujourd'hui	dans 6 ans
fils	x	$x+6$
petit-fils	$x+27$	$x+33$

$$\left. \begin{array}{l} \text{Posons } x+33 = 2(x+6) \\ x+33 = 2x+12 \\ x-2x = 12-33 \end{array} \right\} \begin{array}{l} -x = -21 \\ x = 21 \end{array}$$

fils : 21 ans

petit-fils : 48 ans